

2C.3 WS #3 Graphing Rational Functions

1. Use the rational function $f(x) = \frac{x+2}{x^2-4}$ to complete the following and graph the function. Show all work and label the graph appropriately.

a. Simplify

$$f(x) = \frac{\cancel{x+2}}{(x+2)(x-2)} \quad \text{Hole @ } x = -2$$

b. Domain

all real x , $x \neq -2, 2$

c. Vertical Asymptote(s):

$$x - 2 = 0$$

$x = 2$

d. Horizontal Asymptote:

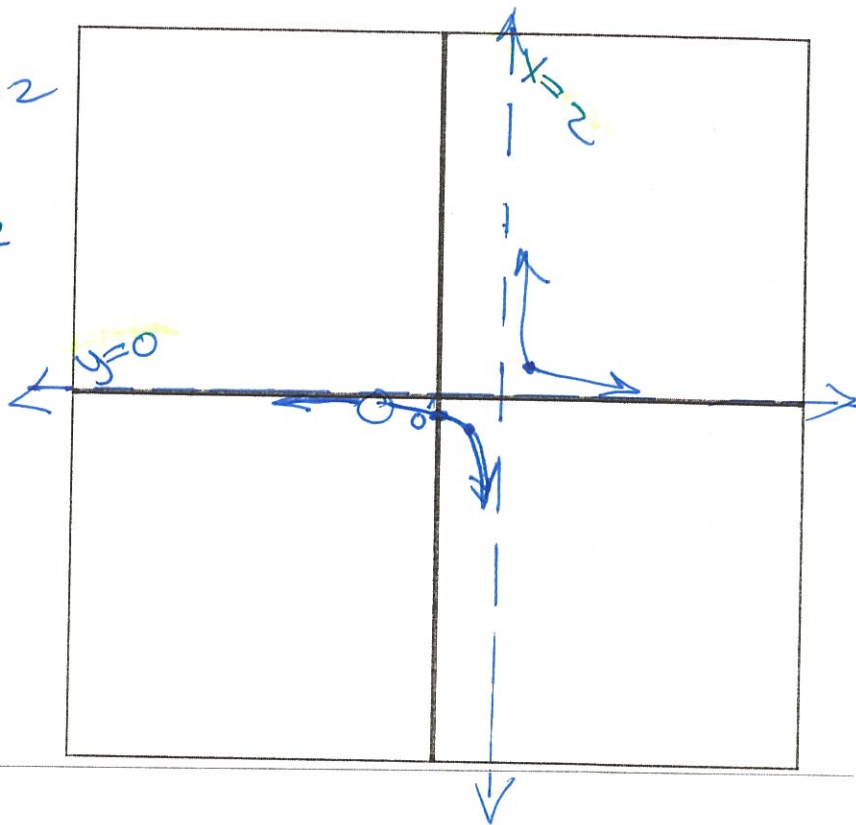
$$n = 1 \quad m = 2$$

$$n < m$$

$y = 0$

e. Slant Asymptote:

NONE



f. x-intercepts

~~$$x + 2 = 0$$

$$x = -2$$~~

HOLE

g. y-intercepts

$$f(0) = \frac{0+2}{0^2-4}$$

$$= -\frac{2}{4}$$

$$(0, -\frac{1}{2})$$

h. Additional Points

x	f(x)
1	-1
3	1

2. Use the rational function $f(x) = \frac{4x-2}{2x+1}$ to complete the following. Show all work and label the graph appropriately.

a. Simplify

$$f(x) = \frac{2(2x-1)}{2x+1}$$

b. Domain

all real x
 $x \neq -\frac{1}{2}$

$2x+1=0$
 $2x=-1$
 $x=-\frac{1}{2}$

c. Vertical Asymptote(s):

$$2x+1=0$$

$$2x=-1$$

$$x = -\frac{1}{2}$$

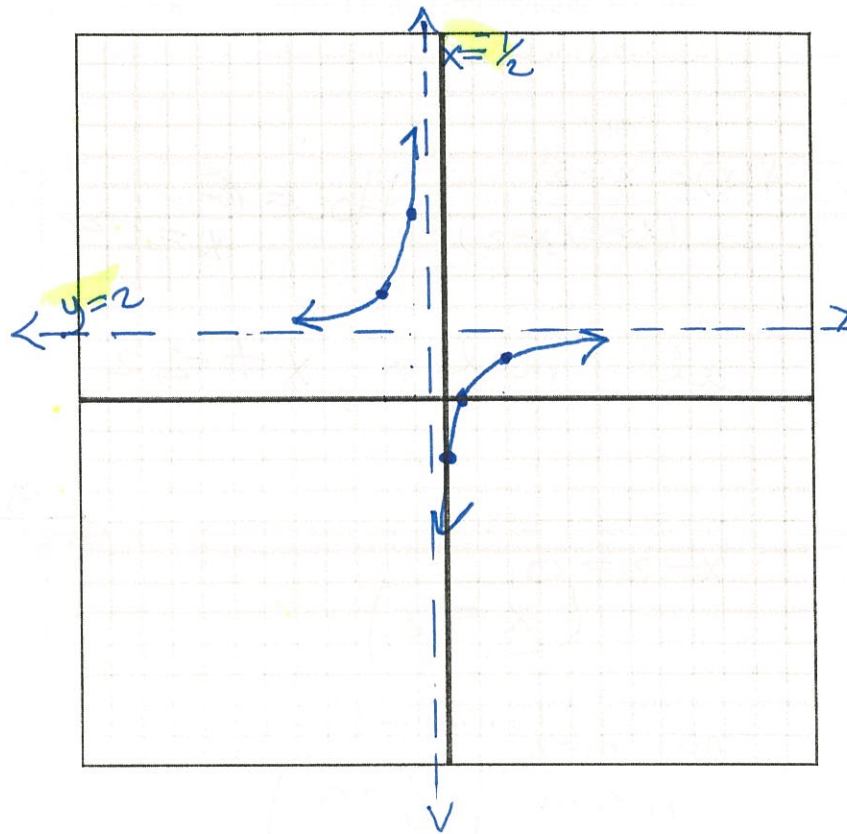
d. Horizontal Asymptote:

$$n=m$$

$$y = \frac{4}{2} = 2$$

e. Slant Asymptote:

NONE



f. x-intercept(s):

$$4x-2=0$$

$$4x=2$$

$$x = \frac{1}{2}$$

$$\left(\frac{1}{2}, 0\right)$$

g. y-intercept(s):

$$f(0) = \frac{4(0)-2}{2(0)+1}$$

$$= -2$$

$$(0, -2)$$

h. Additional Points:

x	$f(x)$
-1	6
-2	3.3
2	1.2